

The 'in virtue of' Relation

EPILOG – Seminar
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The two-factor argument

Quine's view

- A standard analytic truth like $'(x)(x = x)'$.
- It depends on language (on the usage of '=')
- But it is also a fact about the world that $'(x) (x = x)'$

The two-factor argument

Boghossian's view (1997)

- The following schema catches what consists the truth-value of a statement:
- For any S , S is true iff for some p , S means that p and p .

Disambiguating 'in virtue of'

- Analyticity: the meaning determines the truth value of the sentences. We can understand the analyticity in two ways (Quine, Boghossian):
 - The meaning determines totally the T.V. (Absurd)
 - The meaning determines partially the T.V. (Trivial)
- Russell proposes a third way

Disambiguating ‘in virtue of’

- Intuitive grip from arithmetic, the binary multiplication function on **N**:

$$x \times y = z$$

In which way the x-argument determines z?

And the y-argument determines z?

Formal definitions

- Given a function F , we can think F as a Set of n -tuples.
- Ex: binary function on \mathbf{N} is the Set of all triples of number $\langle x, y, z \rangle \in \mathbf{N}$ in which the third member is the result of the first two.
- Ex: for the sentences we can use the M-Function that is the set $\langle m, w, v \rangle$.

1) Partial determination

- definition: an argument place i partially determines the result-place $n + 1$ with respect to a function F just in case there exists a pair of $n + 1$ -tuples $\langle x_1, \dots, x_i, \dots, x_n, y \rangle$,

$$\langle x_1, \dots, x_i', \dots, x_n', y' \rangle \in F$$

such that $x_1 = x_1'$, $x_2 = x_2'$, ..., $x_i \neq x_i'$, ..., $x_n = x_n'$ and $y \neq y'$.

1) Partial determination

The meaning partially determines the T. V.

⟨the proposition that snow is white, wa, T⟩

⟨the proposition that snow is black, wa, F⟩

But also the state of the world

⟨the proposition that snow is white, wa, T⟩

⟨the proposition that snow is white, wb, F⟩

2) Conjoint determination

- definition: a subsequence of argument places, $\langle i, \dots, k \rangle$, conjointly determines the value of a function F just in case there is no pair of n -tuples $\langle x_1, \dots, x_i, \dots, x_k, \dots, x_n, y \rangle$, $\langle x_1', \dots, x_i', \dots, x_k', \dots, x_n', y' \rangle \in F$ such that $\langle x_i, \dots, x_k \rangle = \langle x_i', \dots, x_k' \rangle$ but $y \neq y'$

3) Full determination

- definition: the arguments $x_1 \dots x_k$ in argument positions $i \dots k$ fully determine the result y with respect to a function F just in case for all $n + 1$ -tuples in F , if the values in positions $i \dots k$ are $x_1 \dots x_k$, then the last member of the $n + 1$ -tuple is y .

4) Redundant determination

- definition: an argument x_i in an $n + 1$ - tuple $\langle x_1, \dots, x_i, \dots, x_n, y \rangle$ redundantly determines the result y with respect to a function F just in case (i) the argument place i partially determines the result-position of F , but (ii) there is no $n + 1$ - tuple $\langle x_1', \dots, x_i', \dots, x_n', y' \rangle \in F$ such that $\langle x_1 = x_1', x_2 = x_2', \dots, x_i \neq x_i', \dots, x_n = x_n', \text{ and } y \neq y' \rangle$.

In defense of Analyticity

- Now with these definitions we can try to defend the analytic-synthetic distinction.
- In a **synthetic** sentence the truth-value is fully-determined by neither argument.
- In an **analytic** sentence the truth-value is fully-determined by the meaning of the sentence.

Collapse into necessity?

- Analytic sentences = necessary truths

Collapse into necessity?

- Analytic sentences = necessary truths
 That's a dangerous consequence!
- Sentences expressing substantive necessities
- Contingent analycities

How analyticity doesn't collapse into



- This is not
- re
- W

EPILOG

**EPISODE 3
COMING NEXT WEEK**

Monday
morning on **d.a.f.i.s.t.**

How analyticity doesn't collapse into necessity?

- The *meaning in true in virtue of meaning* is not referring to the content, but to something else.
- What is it?

Thanks for your attention

Bibliography

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